

# Forge: A Cartesian Immersed-Boundary Approach to Unsteady Transonic Flow

*Without Turbulence Modeling, Wall Functions, or Artificial Dissipation*

| Solver         | Description                                              |
|----------------|----------------------------------------------------------|
| Algorithm      | Semi-Lagrangian advection + spectral pressure projection |
| Turbulence     | None (implicit LES)                                      |
| Wall treatment | Physics-based molecular interface model                  |
| Precision      | float64 throughout, PyTorch GPU                          |
| Hardware       | NVIDIA RTX A4000 (16 GB), single GPU                     |
| Implementation | ~3,200 lines Python (one file)                           |

## Precision & Data Integrity

### float64

Every field. Every operation. Every step.

#### Bit-perfect checkpoint resume

Run → stop → restart → identical results

Verified on ONERA OAT15A

#### Full 3D fields saved to HDF5

$u$ ,  $v$ ,  $w$ ,  $p$ ,  $T$ ,  $\rho$ ,  $\text{div}(u)$  per step

LZF compressed. Any quantity

extractable post-hoc.

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| Wall treatment | Physics-based molecular interface model                  |
| Precision      | float64 throughout — no exceptions                       |
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## Globally-synchronized explicit timestep

1. Freeze entire field state at time  $t$
2. Compute ALL domain tendencies simultaneously from that snapshot  
(fluid, thermal, structural, electromagnetic — all see same state)
3. Sum tendencies and project forward once

**No iterative coupling between domains**  
**No matrix inversions or inner iterations**  
**No sequential update contamination**

**Unconditionally stable:  $CFL > 10^{31}$**   
**recorded without divergence**

## Solver Components

| Component   | Approach                                 |
|-------------|------------------------------------------|
| Advection   | Semi-Lagrangian (3D trilinear backtrack) |
| Pressure    | Spectral (FFT) Leray projection          |
| Wall BC     | Molecular accommodation interface        |
| Turbulence  | None — implicit LES from scheme          |
| Dissipation | Zero artificial dissipation              |
| Density     | Active transport + equation of state     |
| Diagnostics | Proprietary info-theoretic scalar        |

## How does it work without a turbulence model?

The wall is not a mathematical boundary condition.  
It is a physics-based interface between two materials.

Momentum exchange is governed by the molecular accommodation coefficient between the fluid and wall material. The velocity field near the wall develops naturally through that exchange — outward through advection and diffusion. No prescribed velocity profile.

### Grid considerations:

Uniform Cartesian. No stretching, no clustering, no aspect ratio management. The consideration is cells per chord and domain extent. Surface interaction is in the interface physics, not in the mesh.

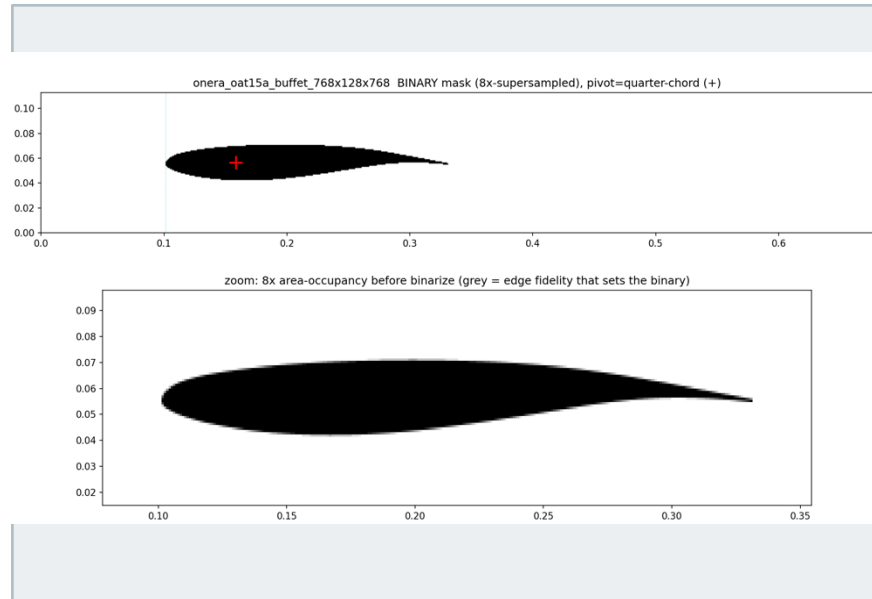
### Conventional vs. Forge

|                    | Conventional                       | Forge                  |
|--------------------|------------------------------------|------------------------|
| <b>Wall BC</b>     | Wall function<br>or $y^+ < 1$      | Molecular<br>interface |
| <b>BL mesh</b>     | 52+ layers<br>$s=1.2$ growth       | Uniform<br>Cartesian   |
| <b>Turb model</b>  | SA, SST $k-\omega$ ,<br>DDES, etc. | None                   |
| <b>Dissipation</b> | Flux limiters,<br>artificial visc. | Zero                   |
| <b>Grid effort</b> | Weeks                              | Minutes                |



## ONERA OAT15A Grid Specification

| Parameter       | Value                  |
|-----------------|------------------------|
| Grid            | 768 × 512 × 16         |
| Total cells     | 6,291,456              |
| dx, dy, dz      | 1.198, 1.797, 1.438 mm |
| Domain          | 0.92 × 0.92 × 0.023 m  |
| Chord (c_ref)   | 230 mm (model scale)   |
| Cells/chord     | ~192 (streamwise)      |
| Surface samples | 17,136                 |
| Span cells      | 16 (10% chord)         |



# ONERA OAT15A: Test Case Setup

| Condition           | Value                   | Source                          |
|---------------------|-------------------------|---------------------------------|
| Mach                | 0.7303                  | DPW-8 TC1                       |
| Angle of attack     | 3.78°                   | Geometry rotated in conversion° |
| $U_\infty$          | 241.0 m/s               | From Mach + $T_{\text{static}}$ |
| $\rho_\infty$       | 0.923 kg/m <sup>3</sup> | Experimental condition          |
| $T_{\text{static}}$ | 271.0 K                 | Experimental condition          |
| $q_\infty$          | 26,804 Pa               | $\frac{1}{2}\rho U^2$           |
| $c_{\text{sound}}$  | 330.0 m/s               | $\sqrt{(\gamma RT)}$            |
| dt                  | $1.0 \times 10^{-4}$ s  | Explicit timestep               |
| Steps analyzed      | 750 (steps 751–1500)    | Post-transient window           |
| Boundary            | Tunnel mode, open walls | Inlet/outlet + open lateral     |

*Note: OAT15A geometry per ONERA designation. Model-scale chord = 230 mm.*

| Quantity | Mean   | Range (unsteady) | $\Delta$ (counts) |
|----------|--------|------------------|-------------------|
| CD       | 0.0389 | 0.0333 – 0.0427  | 94                |
| CL       | 0.1908 | 0.1822 – 0.1973  | 151               |
| CM       | 0.3064 | 0.2906 – 0.3187  | 281               |

1 drag count = 0.0001. CD swing of 94 counts indicates significant unsteady force oscillation.

## Diagnostic convergence (D):

| Step | D      | Status                       |
|------|--------|------------------------------|
| 0    | 0.9997 | Initial (uniform field)      |
| 1    | 0.0632 | 95% resolved                 |
| 5    | 0.0075 | 99.3% resolved               |
| 1500 | 0.0227 | Settled unsteady limit-cycle |

## Spectral characteristics:

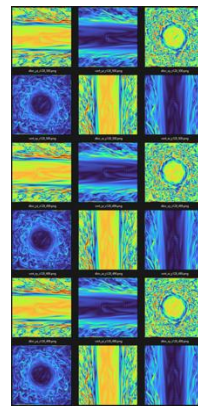
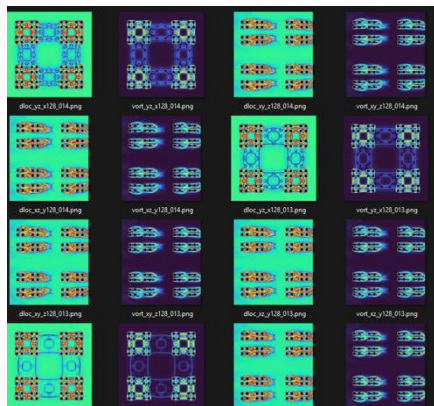
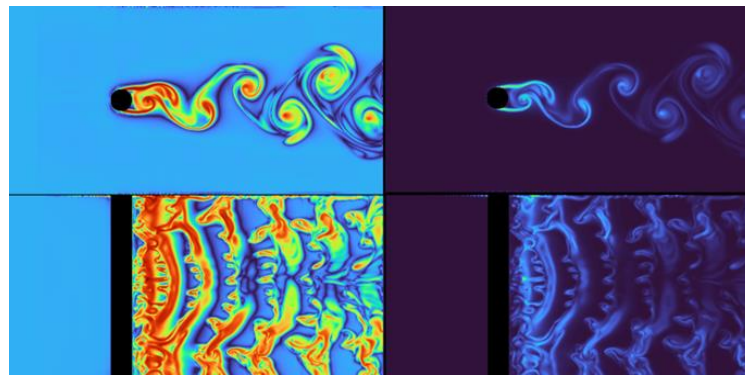
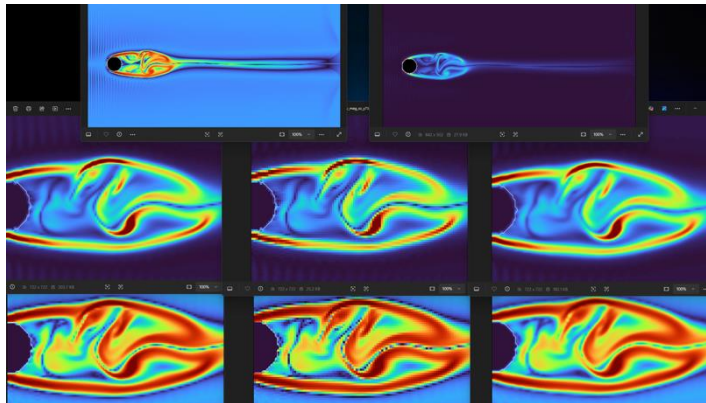
Probe location:  $x/c = 0.45$   
(upper surface, mid-chord)

Analysis window: 750 steps  
 $dt = 1.0 \times 10^{-4}$  s  
Nyquist: 5,000 Hz

**Peak PSD at 13.3 Hz**  
(0.0112 Pa<sup>2</sup>/Hz)

Broadband content above 100 Hz  
consistent with turbulent buffet

*Reference: Jacquin et al. 2009*



## What we showed:

A Cartesian immersed-boundary solver that resolves unsteady transonic flow — including shock buffet — without turbulence modeling, wall functions, or artificial dissipation. Running on consumer workstation hardware.

## Next steps:

Grid refinement studies on ONERA OAT15A  
Full AoA sweep for buffet onset characterization  
NASA CRM force/moment polar completion  
Aeroacoustic analysis from  $\text{div}(\mathbf{u})$  field data

## Post-workshop:

Interested in aligning with the Source of Scatter Working Group and the Buffet Working Group for continued collaboration.

# Thank you

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Questions welcome.