



# **PAB3D simulations for 3<sup>rd</sup> AIAA Drag Prediction Workshop**

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# Presentation Outline

- Introduction
- Governing Equations
- Results and Discussion
- Summary



# Introduction

- Case 1 DLR-F6-WB and FX2B configurations
- Code **PAB3D** structured multi-block
- Grid Boeing grids  
(coarse, medium, medium-fine, & fine)
- Mach = 0.75, Re = 5 million



# Methodology

## PAB3D CFD Code

- 3-D RANS Upwind Code
- Multi-block structured with general patching
- Parallel computing using MPI
- Mesh sequencing
- Low memory requirement
- Graphical user interface (GUI) capabilities
- Linear two-equation  $k-\varepsilon$  models
- Suite of algebraic Reynolds stress models
- LES & PANS



# Governing Equations



## Reynolds (Favre) Averaged Navier-Stokes

### RANS

Continuity	$\frac{\partial \rho}{\partial t} + \frac{\partial \rho u_i}{\partial x_i} = 0$	
Momentum	$\frac{\partial \rho u_i}{\partial t} + \frac{\partial (\rho u_i u_j + p \delta_{ij})}{\partial x_j} = \frac{\partial (\tau_{ij} - \overline{\rho u_i u_j})}{\partial x_j}$	
Energy	$\frac{\partial \rho e_0}{\partial t} + \frac{\partial (\rho e_0 u_i + p u_i)}{\partial x_i} = \frac{\partial (\tau_{ij} u_j - \overline{\rho u_i u_j u_j})}{\partial x_i}$	
	$- \frac{\partial (q_i - C_p \rho \overline{u_i t})}{\partial x_i} - \frac{\overline{\rho u_i u_j u_j}}{2}$	

Reynolds Stress



# Governing Equations

## Two Equation K- ε Model

$$\frac{\partial \rho k}{\partial t} + \frac{\partial \rho u_i k}{\partial x_i} = -\overline{\rho u_i u_j} \frac{\partial u_j}{\partial x_i} + \frac{\partial}{\partial x_i} \left[ \mu_l + \frac{c_\mu k^2}{\sigma_k \varepsilon} \frac{\partial k}{\partial x_i} \right] - \rho \varepsilon (1 + M_\tau^2)$$

$$\frac{\partial \rho \varepsilon}{\partial t} + \frac{\partial \rho u_i \varepsilon}{\partial x_i} = -C_\varepsilon \overline{\rho u_i u_j} \frac{\partial u_j}{\partial x_i} \frac{\varepsilon}{k} + \frac{\partial}{\partial x_i} \left[ \mu_l + \frac{c_\mu k^2}{\sigma_\varepsilon \varepsilon} \frac{\partial \varepsilon}{\partial x_i} \right] - f_2 \tilde{C}_{\varepsilon 2} \rho \frac{\varepsilon}{k} \left[ \varepsilon - v_l \left( \frac{\partial \sqrt{k}}{\partial t} \right)^2 \right]$$

Reynolds Stress

$$C_\mu = .09, C_{\varepsilon 1} = 1.44, \text{ and } \tilde{C}_{\varepsilon 2} = C_{\varepsilon 2} = 1.92$$

Turbulent viscosity: 
$$\nu_t^{RANS} = f_\mu \rho C_\mu \frac{k^2}{\varepsilon}$$



# Governing Equations



## Turbulent Stresses

### Two Equation K- ε Linear Model

(NASA CR-4702, December 1995)

$$-\overline{u_i u_j} = 2\nu_t S_{ij} - \frac{2}{3} \delta_{ij} k$$

### Shih, Zhu, & Lumley (SZL) Nonlinear Model

NASA TM-106644, August 1994

$$-\overline{u_i u_j} = 2\nu_t S_{ij} - \frac{2}{3} \delta_{ij} k - 2\beta \frac{K^3}{\varepsilon^2} (W_{ik} \bar{S}_{kj} - \bar{S}_{ik} W_{kj})$$

### Girimaji Nonlinear Model

ICASE 95-82, December 1995

$$-\overline{u_i u_j} = 2\nu_t S_{ij} - \frac{2}{3} \delta_{ij} k - 2C^* \frac{K^3}{\mu \varepsilon^2} [-G_2 (W_{ik} S_{kj} - S_{ik} W_{kj}) + G_3 (S_{ik} S_{kj} - \frac{1}{3} S_{mn} S_{mn} \delta_{ij})]$$

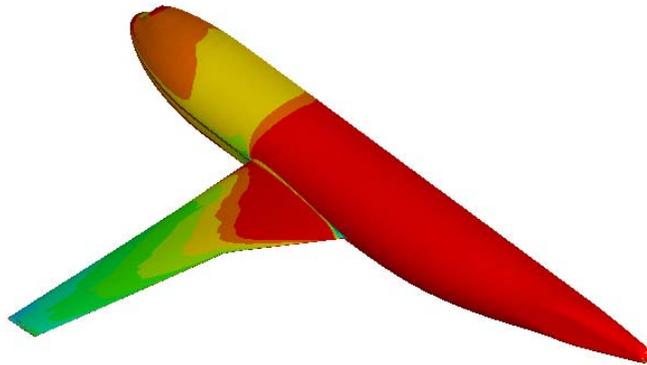
where

$$W_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right) \& \bar{S}_{ij} = S_{ij} - \frac{1}{3} S_{kk} \delta_{ij}$$

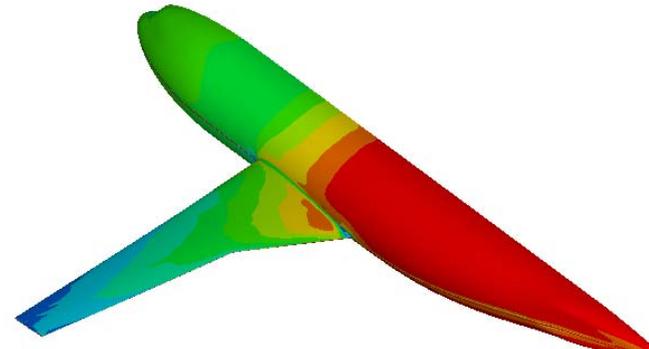


# Computational Grids, Y+

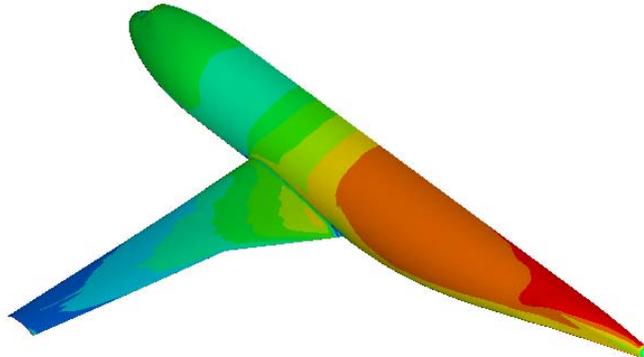
BOEING H-Grids generated by : T.J. Kao and N. J. Yu for Ed. Tinoco



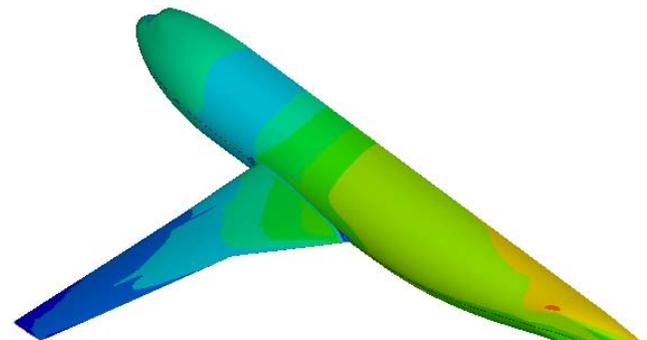
Coarse Grid  
26 Blocks & 2298880 Cells



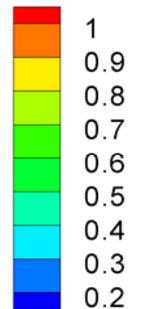
Medium grid  
38 Blocks & 8080896 Cells



Medium-fine grid  
26 Blocks & 15856320 Cells



Fine grid  
57 Blocks & 27185664 Cells





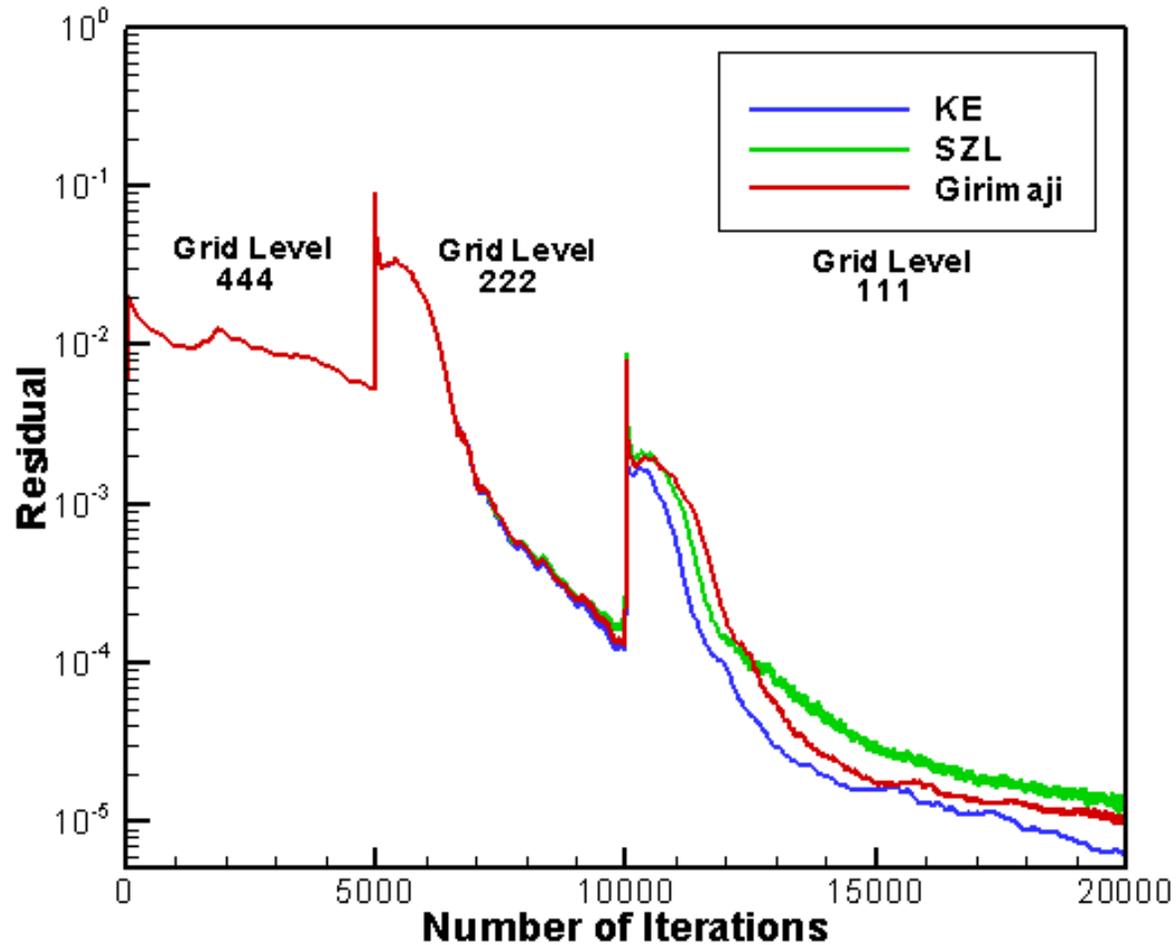
# Case1, F6-WB & FX2B

## Mach 0.75, $Re=5*10^6$

Turbulence Model/ Grid	Coarse	Medium	Medium fine	Fine
k ε	X	X	X	X
SZL	X	X	X	X
Girimaji	X	X	X	X



# Convergence History





# Typical CPU Timings

Grid	Blocks	# of Cell * 10 <sup>6</sup>	Processors	Wall Time	Wall Time /grid point 10 <sup>-6</sup> sec
Coarse	26	2.3 *10 <sup>6</sup>	24	02:02	0.4196472
Medium	38	8.0	38	5.42	0.3032175
Medium fine	49	15.8	46	8:33	0.2713972
Fine	58	27.2	56	17:45	0.2537843



# Grid Convergence, Girimaji

Mach =0.75, Re=5\*10<sup>6</sup>, AOA=0.0

<b>Grid</b>	<b>CL</b>	<b>CD</b>	<b>CM_TOT</b>
<b>Coarse</b>	<b>0.496</b>	<b>0.03224</b>	<b>-0.1227</b>
<b>Medium</b>	<b>0.487</b>	<b>0.02833</b>	<b>-0.1362</b>
<b>Medium fine</b>	<b>0.485</b>	<b>0.02743</b>	<b>-0.1377</b>
<b>Fine</b>	<b>0.485</b>	<b>0.02728</b>	<b>-0.1378</b>



# Turbulence Model Effect

Mach =0.75, Re=5\*10<sup>6</sup>, AOA=0.0

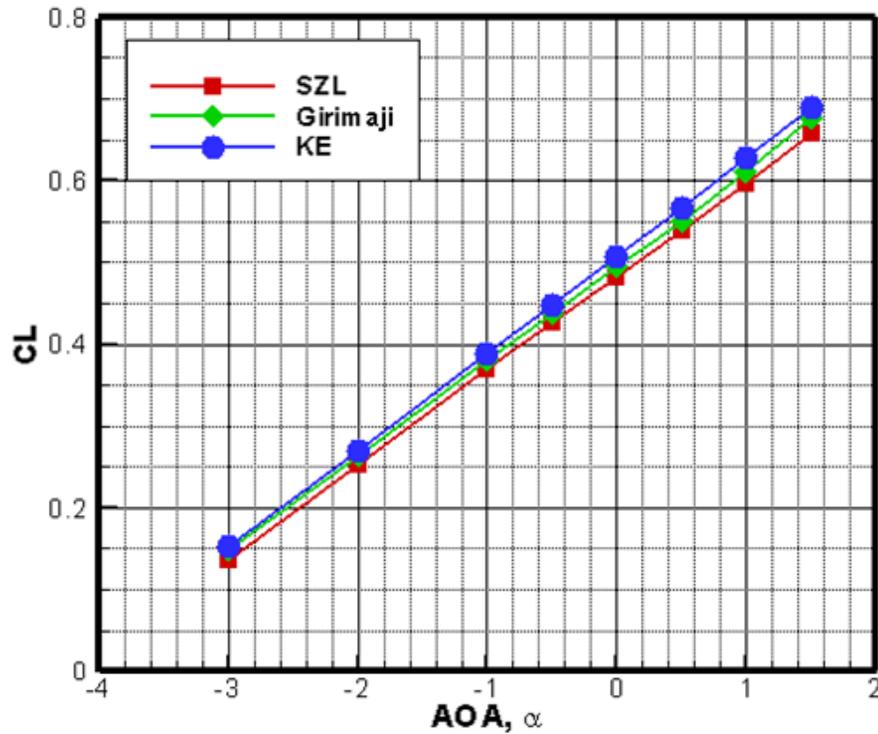
<b>Grid</b>	<b>CL</b>	<b>CD</b>	<b>CM_TOT</b>
<b>KE</b>	0.499	0.03086	-0.1427
<b>SZL</b>	0.477	0.02630	-0.1324
<b>Girimaji</b>	0.485	0.02728	-0.1378



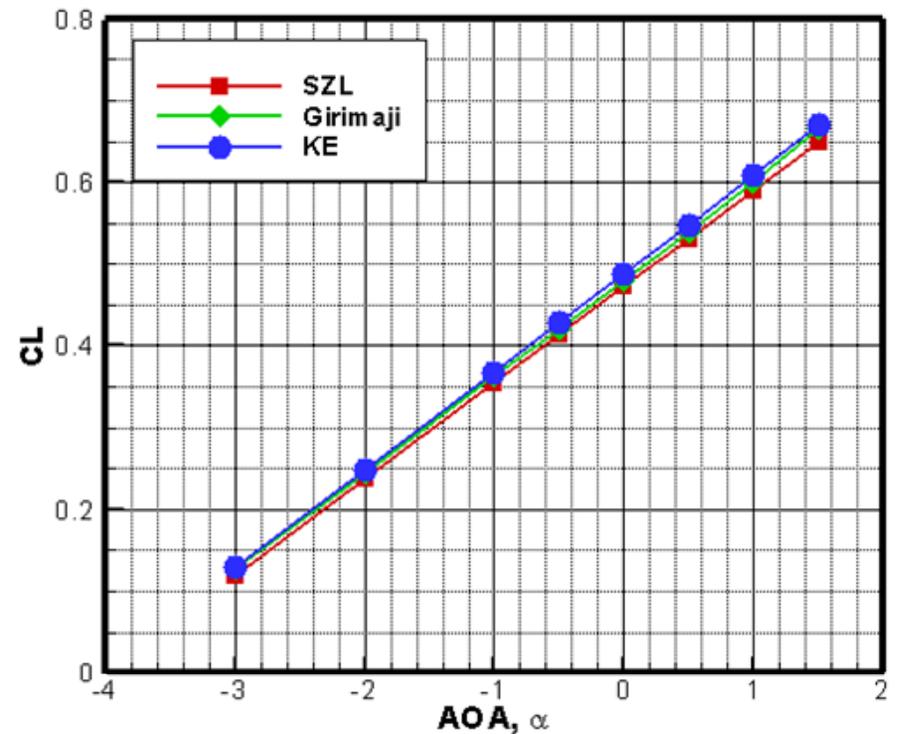
# Lift Curve on Medium Grids



Mach =0.75, Re=5\*10<sup>6</sup>



F6-WB



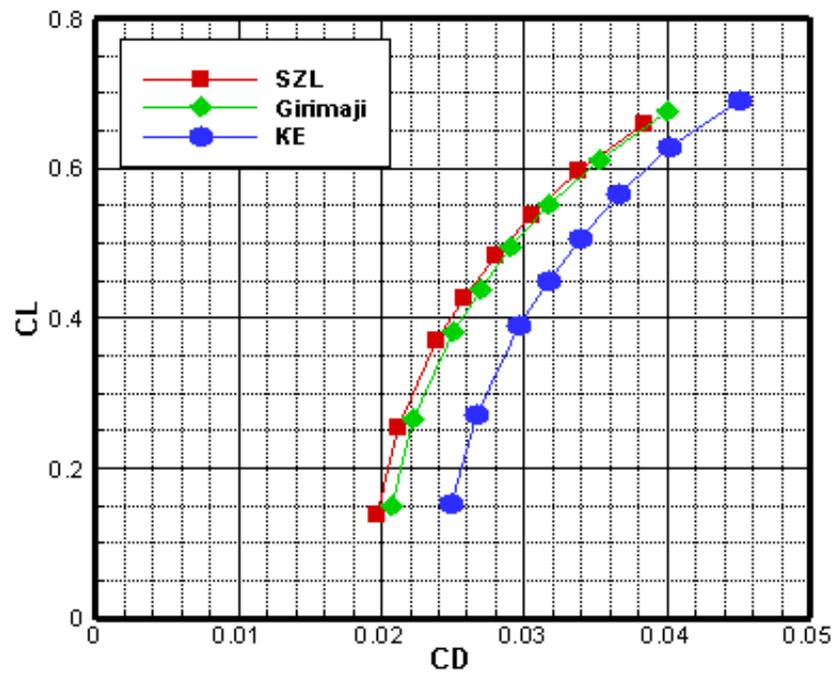
FX2B



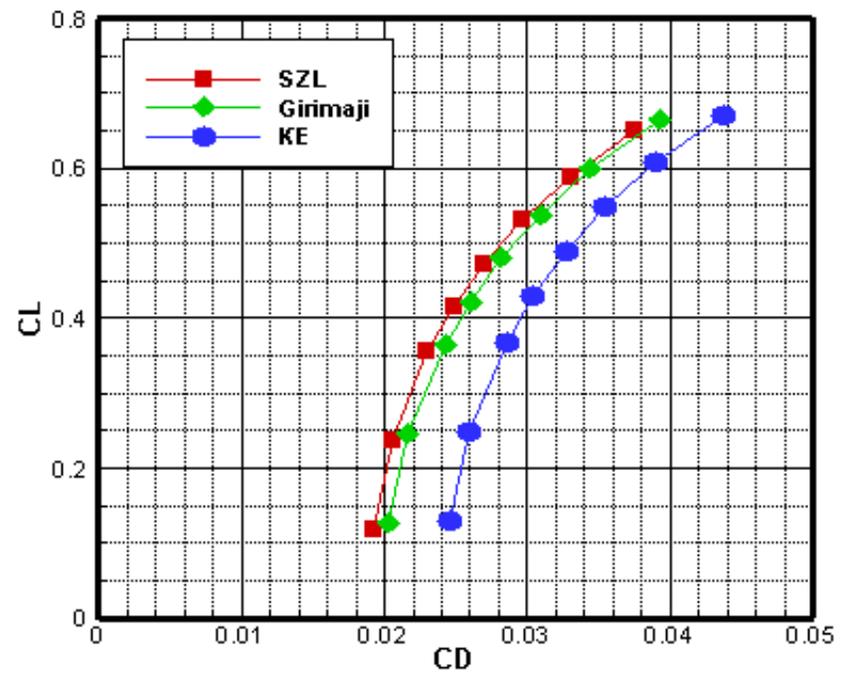
# Drag Polar on Medium Grids



Mach =0.75, Re=5\*10<sup>6</sup>



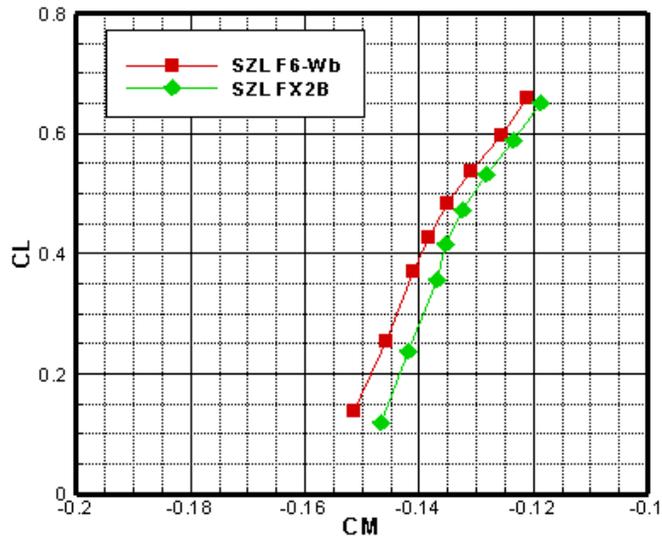
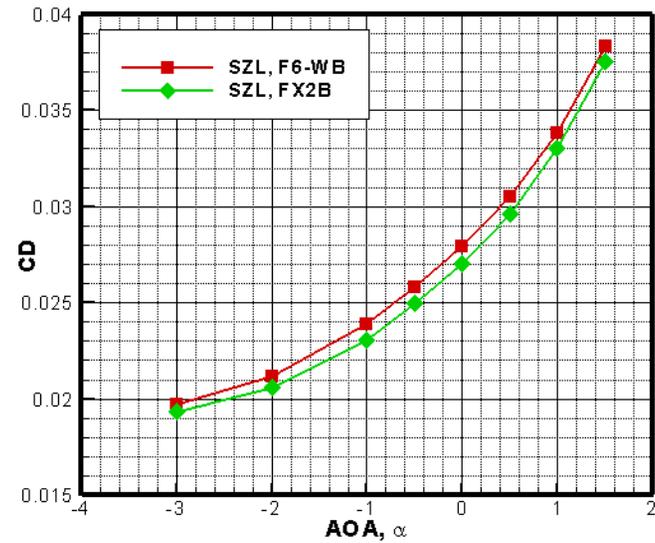
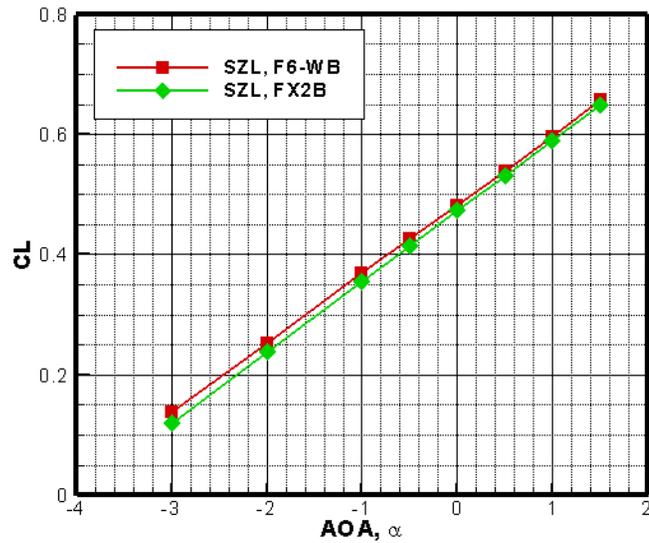
F6-WB



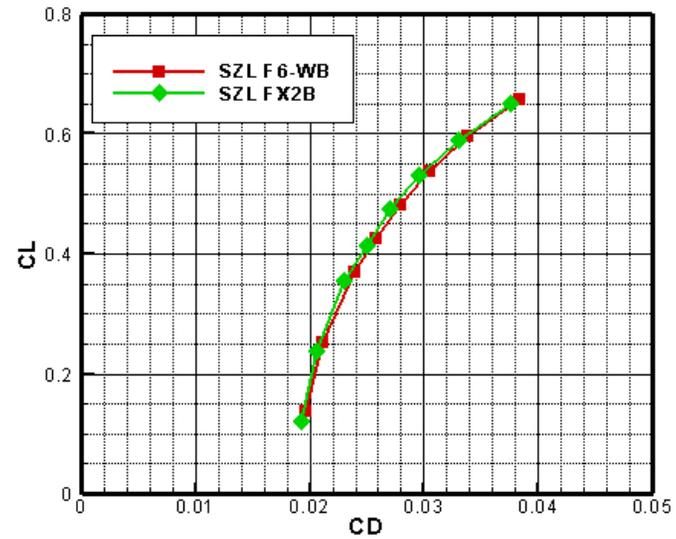
FX2B



# F6\_WB and FX2B Comparison, SZL



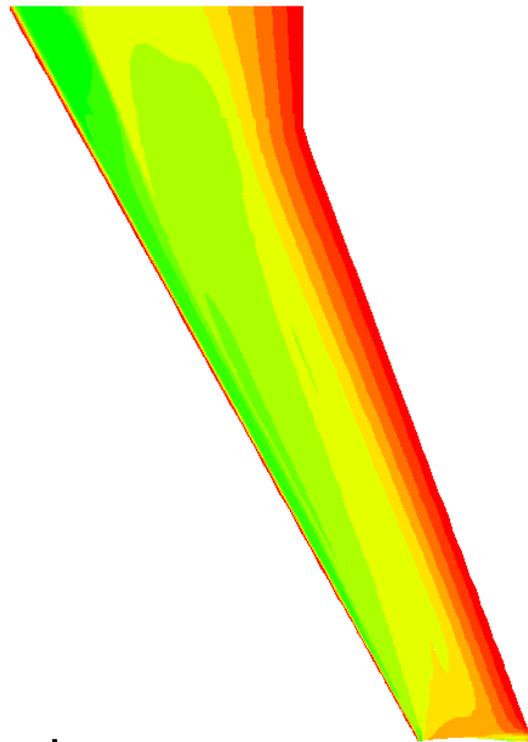
direction 1



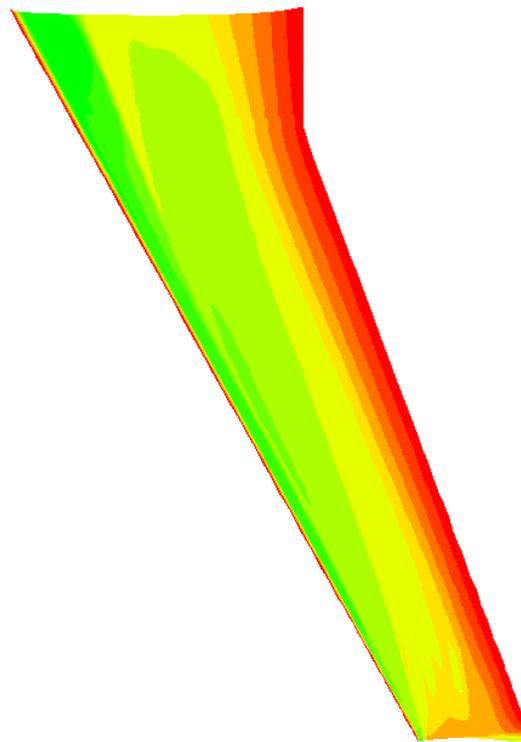


# Coefficient of Pressure

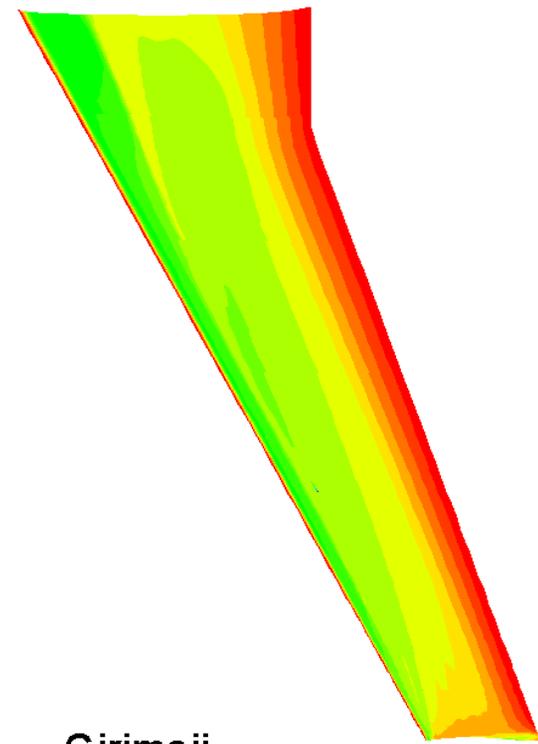
Mach = 0.75,  $Re = 5 \cdot 10^6$ , AOA = 0.0



**kε**



**SZL**



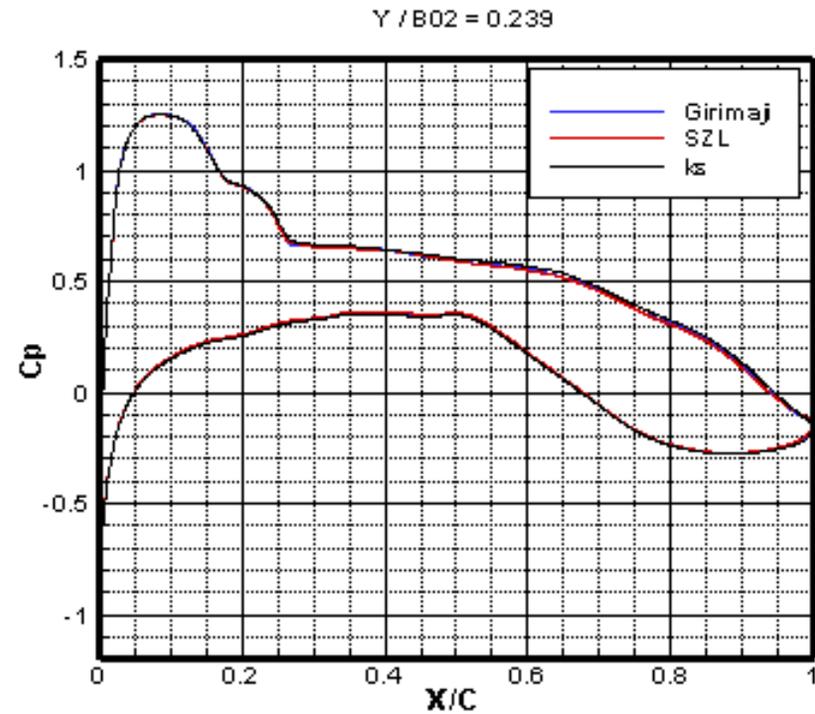
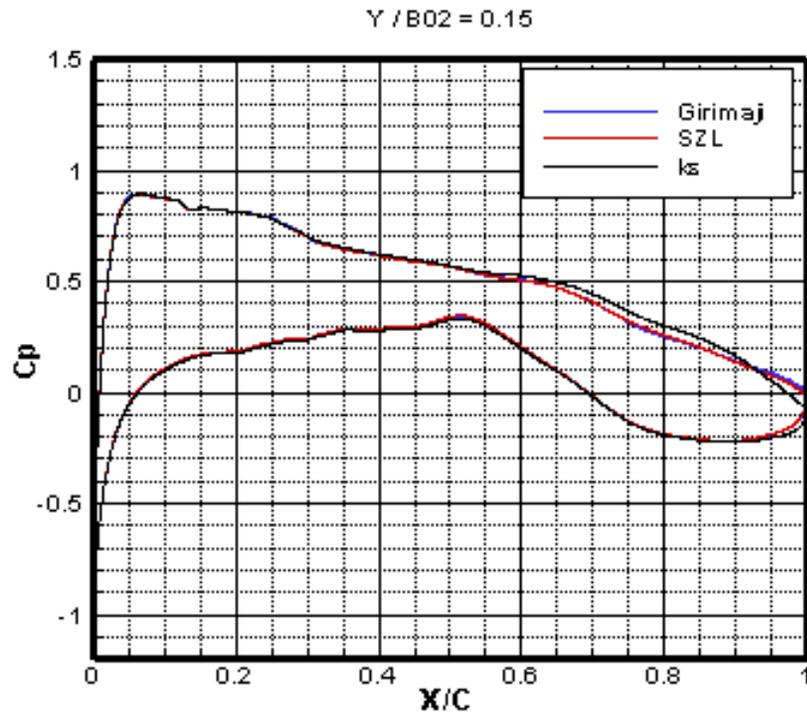
**Girimaji**



# Turbulence Model Effect on $C_p$



Mach = 0.75,  $Re = 5 \cdot 10^6$ , AOA = 0.0

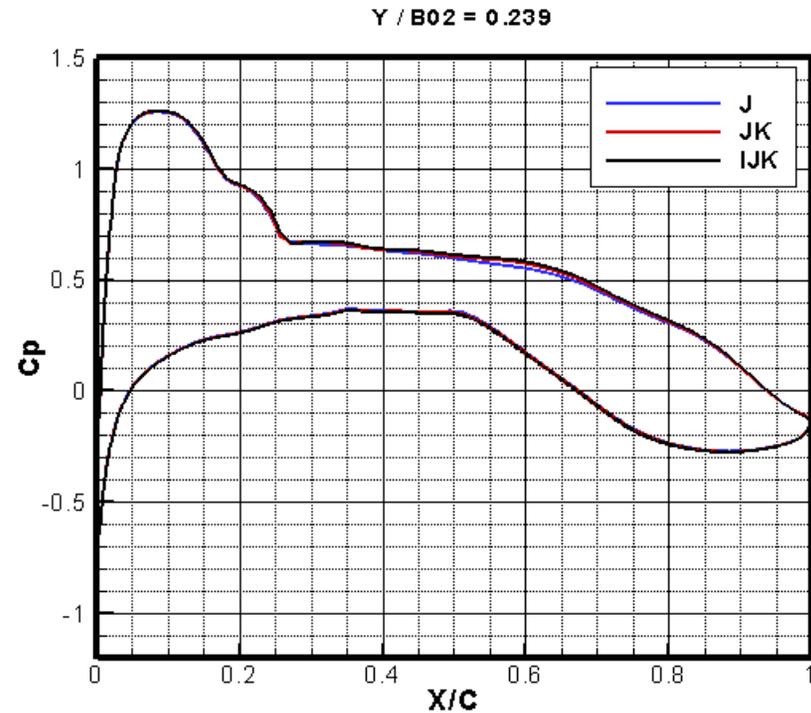
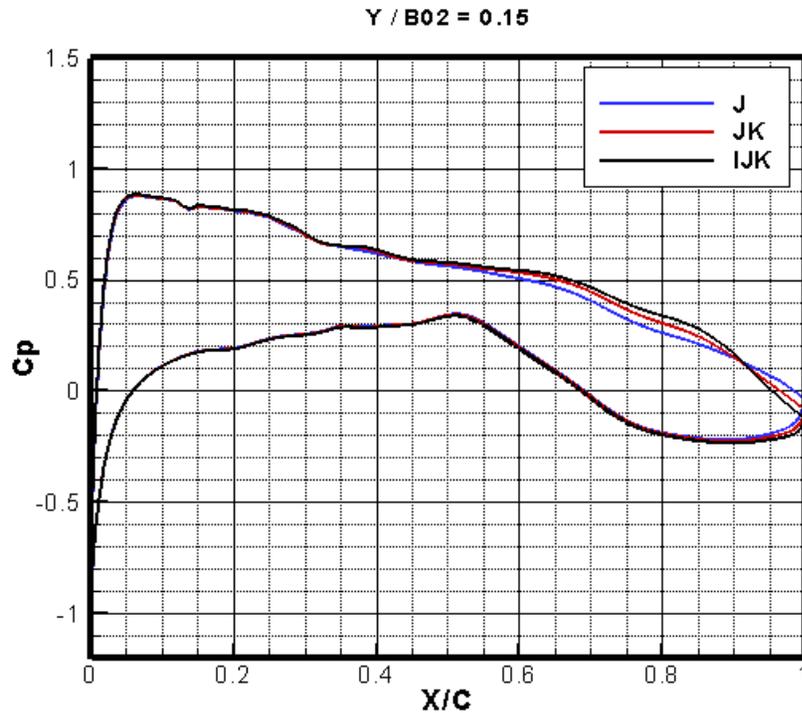




# Thin Shear Layer Effect on Cp



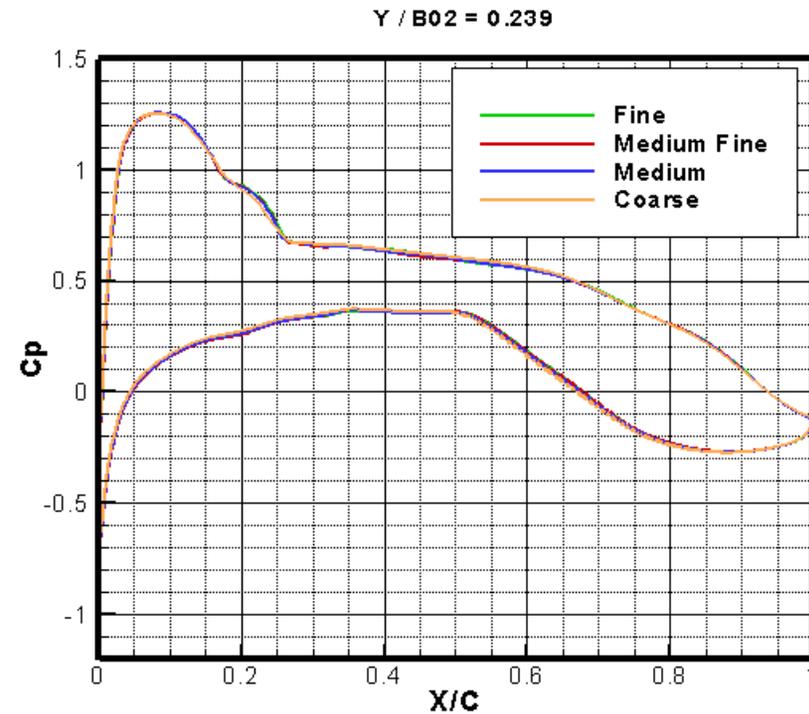
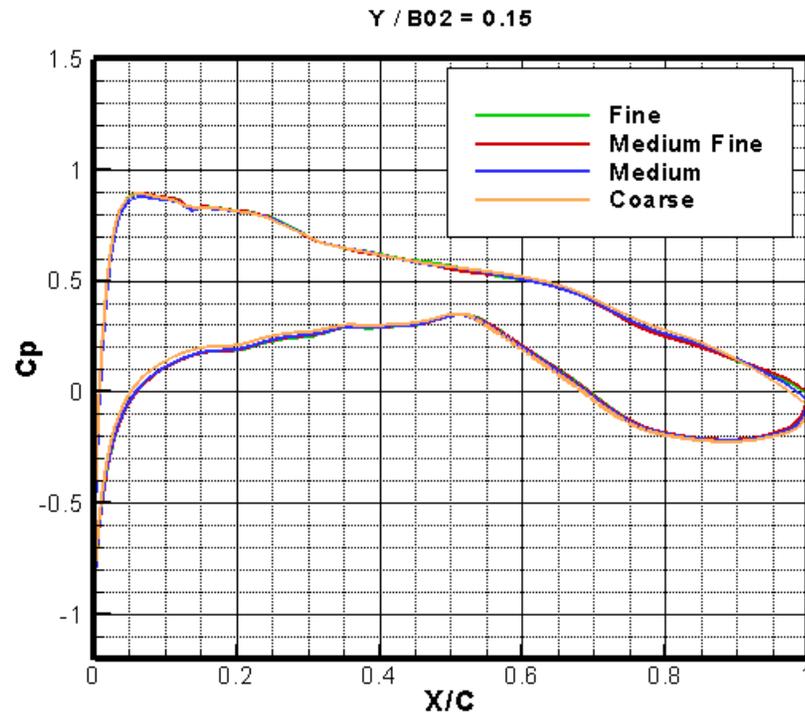
Mach = 0.75,  $Re = 5 \cdot 10^6$ , AOA = 0.0, SZL





# Grid Effect on Cp

Mach = 0.75,  $Re=5 \cdot 10^6$ , AOA=0.0

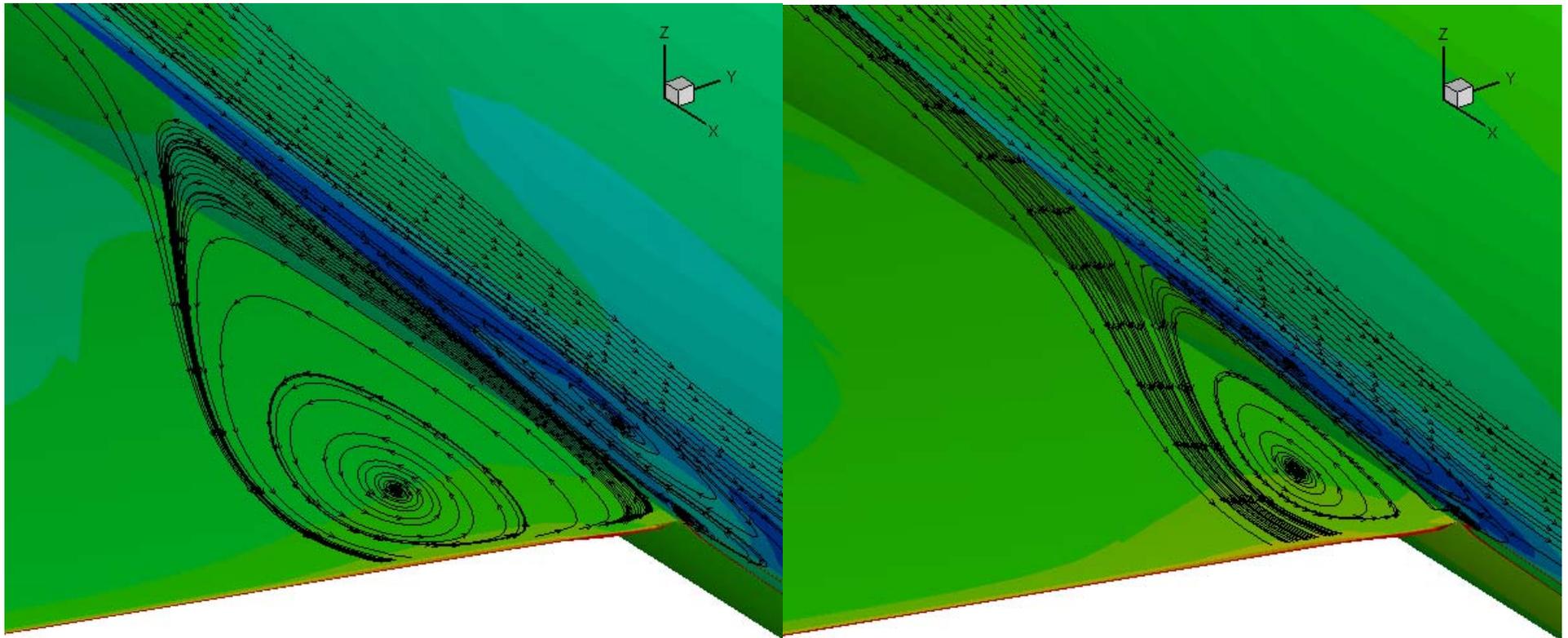




# Upper Wing Streamlines, F6-WB



Mach =0.75,  $Re=5 \cdot 10^6$ , AOA=0.0



SZL medium grid  
Thin Shear Layer in 2 directions

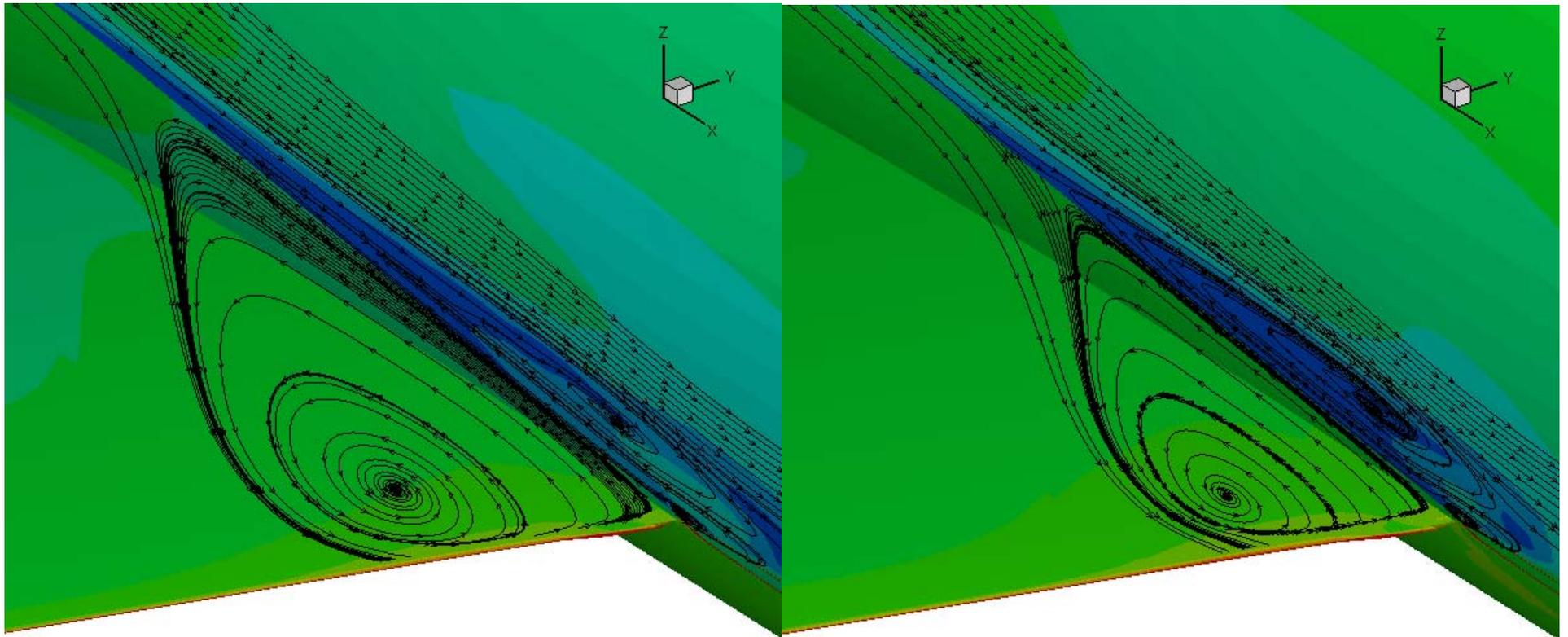
$k\epsilon$  medium grid  
Thin Shear Layer in 2 directions



# Upper Wing Streamlines, F6-WB



Mach =0.75,  $Re=5 \cdot 10^6$ , AOA=0.0



SZL medium grid

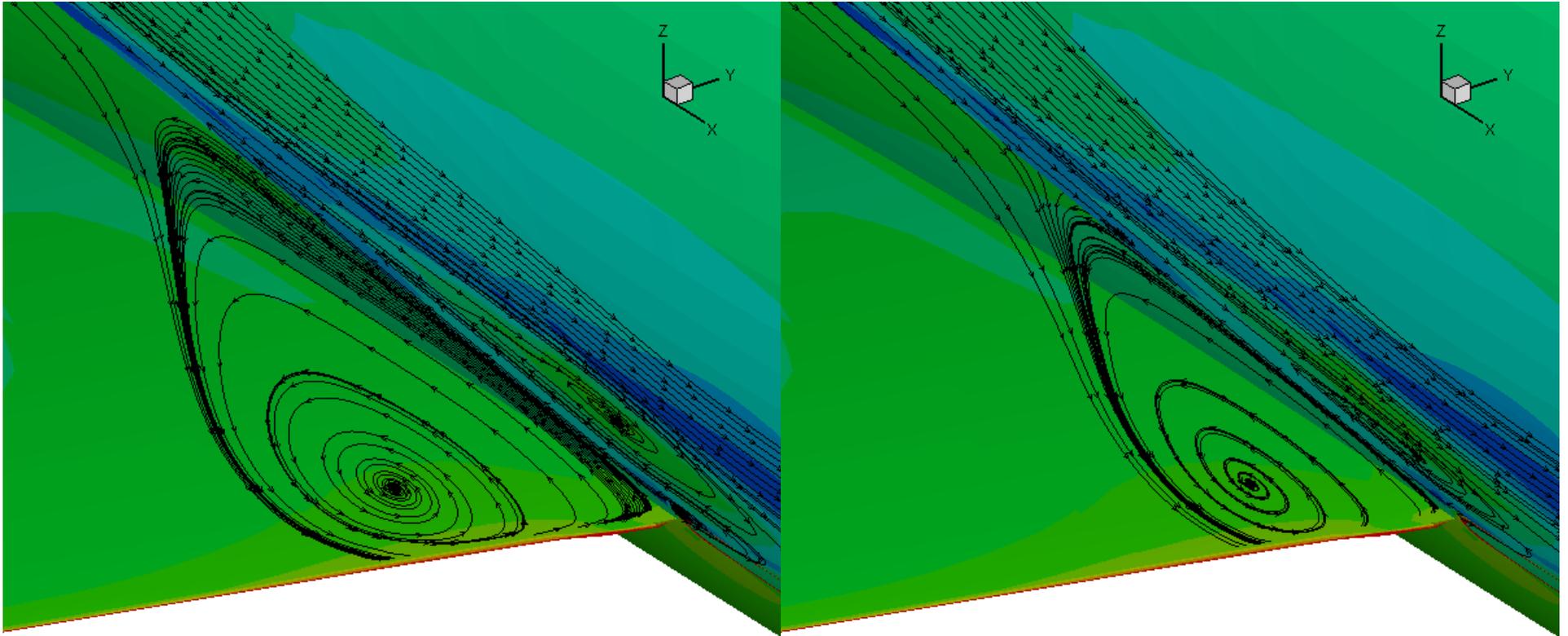
Girimaji medium grid



# Upper Wing Streamlines, F6-WB



Mach =0.75,  $Re=5*10^6$ , AOA=0.0, SZL



Thin Shear Layer in 2 directions, JK

Thin Shear Layer in 3 directions, IJK



# Summary

- PAB3D was utilized to compute the flow field of DLR F6-Wb & FX2B
- Three different turbulence Models and four different grid resolutions were utilized
- AS expected  $k\epsilon$  models produced the highest skin friction
- SZL & Girmaji algebraic Reynolds Stress models predicts similar separation bubbles
- Turbulence model affects size of separation bubble.
- Same suite of algebraic Reynolds Stress models are ported into USM3D

Need to develop innovative turbulence models for flow separation  
and  
implement the models within state-of-the-art RANS flow solvers